

acm international collegiate programming contest INDONESIA NATIONAL CONTEST INC 2018



# Problem L Fair Tournament

Ayu was participating in Asian Championship for Mind Sports (ACMS) 2018, a competition where the (supposedly) best mind triumphs. This competition uses a knockout-tournament system with  $2^N$  players. A match is played by two opposing players and its result cannot be a tie (i.e. there's always a winner). In the first round, the  $1^{st}$  player will compete against the  $2^{nd}$  player, the  $3^{rd}$  player will compete against the  $4^{th}$  player, the  $5^{th}$  player will compete against the  $6^{th}$  player, and so on. On the second round, the winner of the first match ( $1^{st}$  or  $2^{nd}$  player) will compete against the winner of the second match ( $3^{rd}$  or  $4^{th}$  player), and so on. At the last/final round, there will be only two players competing against each other, and there will be one champion.

Needless to say, the ACMS 2018's champion is Ayu!

Budi, who knows Ayu pretty well, doesn't believe this fact. He suspects the competition was rigged. Budi also knows all other contestants, and he's pretty sure these contestants will not cheat or fix any match. So, the only possible set-up is on the organizer side.

Budi has computed a matrix A of  $2^N \times 2^N$ . If  $A_{ij}$  is positive, then the  $i^{th}$  player will win against the  $j^{th}$  with an effort of  $A_{ij}$ , if they have a match. On the other hand, if  $A_{ij}$  is negative, then the  $i^{th}$  player will lose against the  $j^{th}$  player in a match; in this case, the absolute value means nothing. Of course,  $A_{ii}$  will be zero while all other elements are non-zero. It is guaranteed that exactly one of  $A_{ij}$  and  $A_{ji}$  will be positive for  $i \neq j$ . The total effort of a player to win the tournament is defined as the sum of all efforts he/she spent in all of his/her matches.

Budi believes that the organizer fixed the initial players/matches arrangement for the first round such that Ayu will win the tournament with the minimum total effort spent. Notice that for a tournament with M player, there are M! arrangements can be made for the first round.

Given the matrix A, your task is to find the players arrangement such that Ayu (the  $1^{st}$  player) wins the tournament with the minimum possible total effort. Output only the total effort. If it's not possible for Ayu to win the tournament, output -1 instead.

# Input

Input begins with an integer N ( $1 \le N \le 4$ ) in a line. The next  $2^N$  lines, each contains  $2^N$  integers:  $A_{ij}$  ( $-1 \le A_{ij} \le 10^6$ ;  $A_{ii} = 0$ ;  $i \ne j \implies A_{ij} \ne 0$ ). It is guaranteed that exactly one of  $A_{ij}$  and  $A_{ji}$  will be positive for  $i \ne j$ . The entries for  $A_1$  correspond to Ayu.

# Output

Output in a line the minimum total effort needed by Ayu to win the tournament.





## Sample Input #1

0

## Sample Output #1

3

Explanation for the sample input/output #1

There are 4! = 24 initial arrangements can be made for the first round. Some of them are:

- (1, 2, 3, 4). Ayu wins against the  $2^{nd}$  player with an effort of 1. The  $3^{rd}$  player wins against the  $4^{th}$  player with an effort of 3. On the final round, Ayu wins against the  $3^{rd}$  player with an effort of 7. The total effort spent by Ayu is 1 + 7 = 8.
- (3, 1, 2, 4). Ayu wins against the  $3^{rd}$  player with an effort of 7. The  $2^{nd}$  player wins against the  $4^{th}$  player with an effort of 2. On the final round, Ayu wins against the  $2^{nd}$  player with an effort of 1. The total effort spent by Ayu is 7 + 1 = 8.
- (2, 3, 1, 4). The  $2^{nd}$  player wins against the  $3^{rd}$  player with an effort of 4. Ayu wins against the  $4^{th}$  player with an effort of 2. On the final round, Ayu wins against the  $2^{nd}$  player with an effort of 1. The total effort spent by Ayu is 2 + 1 = 3.

Among all possible permutations for the first round, the minimum possible for Ayu's total effort to win the tournament is 3.

## Sample Input #2

1		
0 -1		
3 0		

## Sample Output #2

-1

Explanation for the sample input/output #2

There is no way Ayu can win the tournament.

<sup>• ...</sup>