

# Problem J Super Sum

In this problem, you are given *N* tuples (a, b, c), where *a*, *b*, and *c*, are integers and  $b \le c$ , your task is to compute the **sum** of all the following terms:

 $a_1^{d_1} \times a_2^{d_2} \times ... \times a_N^{d_N}$  for every combination of integer  $d_k$  in  $b_k \le d_k \le c_k$ 

For example, let *N* be 3 and the tuples are: (2,1,3), (3,3,4), and (5,0,1). Then,

| • $2^1 \times 3^3 \times 5^0 = 54$  | • $2^2 \times 3^3 \times 5^0 = 108$  | • $2^3 \times 3^3 \times 5^0 = 216$         |
|-------------------------------------|--------------------------------------|---|
| • $2^1 \times 3^3 \times 5^1 = 270$ | • $2^2 \times 3^3 \times 5^1 = 540$  | • $2^3 \times 3^3 \times 5^1 = 1080$        |
| • $2^1 \times 3^4 \times 5^0 = 162$ | • $2^2 \times 3^4 \times 5^0 = 324$  | $\bullet \ 2^3 \times 3^4 \times 5^0 = 648$ |
| • $2^1 \times 3^4 \times 5^1 = 810$ | • $2^2 \times 3^4 \times 5^1 = 1620$ | • $2^3 \times 3^4 \times 5^1 = 3240$        |
|                                     |                                      |   |

and the sum is: 54 + 270 + 162 + 810 + 108 + 540 + 324 + 1620 + 216 + 1080 + 648 + 3240 = 9072.

#### Input

The first line of input contains an integer T ( $T \le 100$ ) denoting the number of cases. Each case begins with an integer N ( $1 \le N \le 100$ ) denoting the number of tuple. The next N following lines, each contains three integers:  $a \ b \ c \ (1 \le a \le 10^9; \ 0 \le b \le c \le 10^9)$  representing the given tuple.

#### Output

For each case, output "Case #x: y" (without quotes) in a line where x is the case number (starts from 1), and y is the answer for this particular case modulo 1,000,000,007.

| Sample Input  | Output for Sample Input   |
|---|---|
| 4<br>3<br>2 1 3<br>3 3 4<br>5 0 1<br>3<br>5 2 3<br>2 1 4<br>3 2 2<br>1<br>7 0 0<br>2<br>10 3 5<br>3 1 2 | Case #1: 9072<br>Case #2: 40500<br>Case #3: 1<br>Case #4: 1332000 |



#### Explanation for 1<sup>st</sup> sample case

This is the example given in the problem statement.

### Explanation for 2<sup>nd</sup> sample case

In this case, you should compute the sum of all the following terms:

- $5^2 \times 2^1 \times 3^2 = 450$
- $5^2 \times 2^2 \times 3^2 = 900$
- $5^2 \times 2^3 \times 3^2 = 1800$
- $5^2 \times 2^4 \times 3^2 = 3600$
- $5^3 \times 2^1 \times 3^2 = 2250$ •  $5^3 \times 2^2 \times 3^2 = 4500$ •  $5^3 \times 2^3 \times 3^2 = 9000$ •  $5^3 \times 2^4 \times 3^2 = 18000$

•  $5^3 \times 2^1 \times 3^2 = 2250$ 

and the sum is 40500.

# Explanation for 3<sup>rd</sup> sample case

In this case, you should compute the sum of all the following terms:

•  $7^0 = 1$ 

and the sum is 1.

## Explanation for 4<sup>th</sup> sample case

In this case, you should compute the sum of all the following terms:

- $10^3 \times 3^1 = 3000$
- $10^3 \times 3^2 = 9000$
- $10^4 \times 3^1 = 30000$
- $10^4 \times 3^2 = 90000$
- $10^5 \times 3^1 = 300000$
- $10^5 \times 3^2 = 900000$

and the sum is 1332000.